

# **SIMPLE MODEL FOR PRYING FORCES IN T-HANGER CONNECTIONS WITH SNUG TIGHTENED BOLTS**

**By**

**Fathy Abdelmoniem Abdelfattah**  
Faculty of Engineering at Shoubra,  
Zagazig University, Banha Branch

**Mohamed Salah A. Soliman**  
Faculty of Engineering at Shoubra,  
Zagazig University, Banha Branch

## **ABSTRACT**

A simple model for evaluating prying forces in T - hanger connection with snug tightened bolts is proposed. The model includes the flexural stiffness of the flanges and the axial stiffness of the bolts. It is valid as far as the connection behaves in an elastic manner. Prying forces' values were obtained from this analysis and compared to those obtained from the proposed model. The obtained results show good agreement and verify the adequacy of the proposed model. A parametric study was carried out. The effects of the different geometrical properties of the connection on prying force values have been presented and discussed. Design procedure is proposed.

## **KEY WORDS**

Connections , tension , T - hanger, prying force, bolts, snug tightened

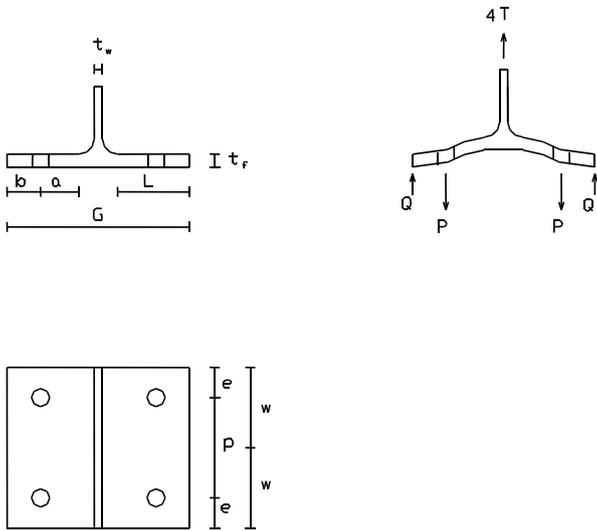
## **INTRODUCTION**

Hanger type connections are employed in steel structures to transmit tension forces. Four bolts are normally used in this type of connection and positioned in two rows symmetrical about the web, **Fig. 1**. Due to connection displacements and deformations, flanges may react against their base. This would induce forces at these positions called prying forces. The magnitudes of these forces depend on the flexure stiffness of the flanges and the axial stiffness of the bolts, (Faella et. al. 1998 and Fleischman et. al. 1991). The bolts are required to resist both the applied tension force and the induced prying forces.

Several relationships have been suggested in the literature to determine the magnitude of prying forces, (Douty et. al. 1965, Kato et. al. 1973 and Agerskov 1976). However, these relations were derived assuming that bolts are preloaded to their full proof loads. Prying force magnitude is related in this case to bolts' separations, bolts yielding and/or the development of the flanges plastic moment. For allowable stress design, The model provided in the 8th edition of the American Institute of Steel Construction manual (AISC 1980) can be used. This model was recommended before by (Fisher and Struik 1974). Later, this model was modified by (Astaneh 1985 and Thornton 1985) to avoid the iterative process required to obtain simpler design procedure. The two major independent failure modes considered in this model are the

flanges and the bolts' failures. It is assumed that equal critical moments exit at the face of the web and at the bolt line, (AISC 1980). This moment is equal to half the plastic moment of the flange. Bolt's failure is limited by their allowable loads. The prying forces' values calculated using this model satisfy these limit conditions. The procedure in general is a limit state design method.

In this paper, The authors propose a simple model for evaluating prying forces in T - hanger connections with snug tightened bolts. The model includes the flexural stiffness of the flanges and the axial stiffness of the bolts. It is valid as far as the connection behaves in an elastic manner. The obtained values of prying forces are not affected by the change in the yield strength of the flanges material and/or the allowable load of the bolts. The finite element method was also used to model the behavior of T - hanger connections. The prying forces values were obtained from this analysis and compared to those obtained from the proposed model. A parametric study was carried out. The results are presented and discussed to indicate the effects of the different parameters on prying forces' values. Design procedure is proposed and the results are compared to those of the (AISC 1980)



(a) geometrical details. (b) deformed shape.

Fig. 1 T - hanger connections.

**PROPOSED MODEL**

This model is proposed for calculating prying action in T - hanger connections with snug tightened bolts. The small deflection theory is employed. Due to the symmetry about two axes, only quarter of the connection is considered. The following equations are derived for one bolt and its associated flange. The interaction behavior of the flange and its associated bolt is modeled by the structure shown in **Fig. 2**. The flange acts as a beam fixed against rotation and free to translate vertically at point C. Further, it is supported by spring against translating at point B. The active span of the beam is made equal to L.

$$L = \{ G - ( 2 r + t_w ) \} / 2 \tag{1}$$

$$\alpha = a / L \tag{2}$$

$$\beta = b / L \tag{3}$$

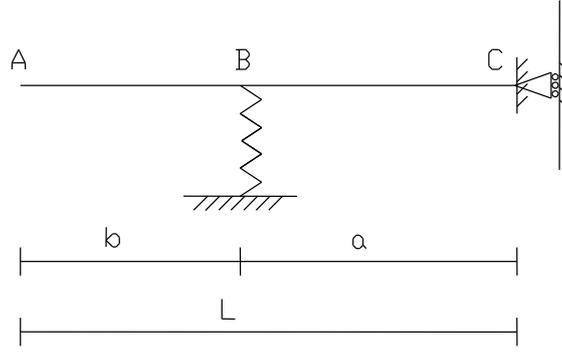


Fig. 2 Simple model for T-hanger connections.

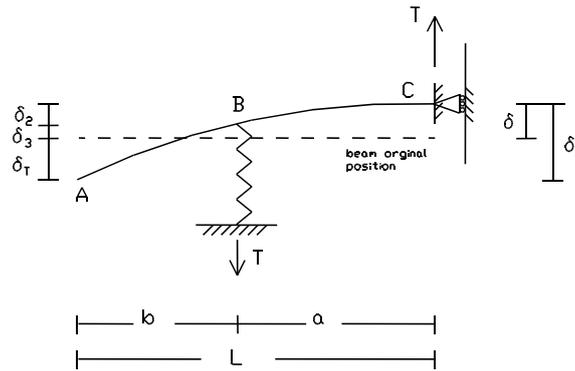


Fig. 3 Modeling the applied tension force.

Where  $G$  is the flange width,  $r$  is the fillet radius and  $t_w$  is the web thickness. The values of  $a$  and  $b$  define the position of bolt hole center. The symbols  $T$  and  $Q$  denote the applied tension force and induced prying force per bolt respectively.

When  $T$  is applied, point  $C$  translates distance  $\delta$  and the spring elongates distance  $\delta_3$ . The beam deforms as a cantilever, **Fig. 3**. The deflection of point  $A$  is expressed as

$$\delta_T = \delta_1 - (\delta_2 + \delta_3) \quad (4)$$

By using the deflection equation of cantilever, the following equations are obtained.

$$\delta_1 = (T L^3 \alpha^2 / 6 E I) (3 - \alpha) \quad (5)$$

$$\delta_2 = 2 T L^3 \alpha^3 / 6 E I \quad (6)$$

$$I = w t_f^3 / 12 \quad (7)$$

and 
$$\delta_3 = T / (E_b A_b / L_b) \quad (8)$$

Where  $E$  and  $E_b$  are the modulus of elasticity of the flange and the bolt materials respectively,  $w$  is the flange length per bolt,  $t_f$  is the flange thickness,  $A_b$  is the bolt cross sectional area and  $L_b$  is bolt grip length. When using the terms:

$$J = L^3 / 6 E I \quad (9)$$

$$K_b = E_b A_b / L_b \quad (10)$$

and applying equations (5), (6) and (8) in equation (4), the value of  $\delta_T$  can be expressed as:

$$\delta_T = T \{ 3 J \alpha^2 \beta - (1 / K_b) \} \quad (11)$$

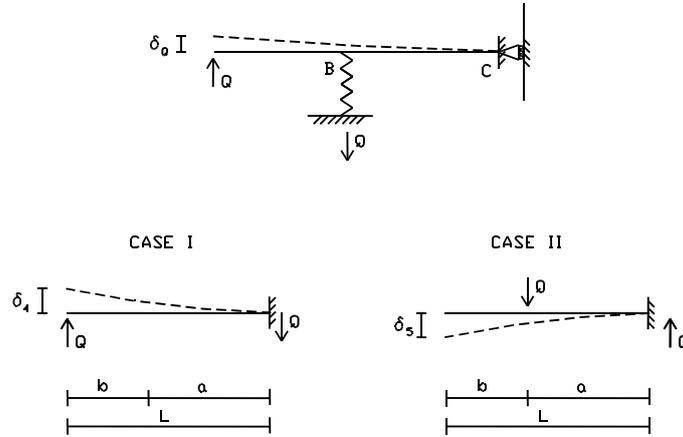


Fig. 4 Modeling the induced prying force.

Prying force is assumed to act as shown in **Fig. 4**. It is assumed that point C does not displace from its position. The problem is resolved in two cases, I and II, as shown in **Fig.4**. The spring supporting condition is not considered in this stage. The flange is dealt with as a cantilever having an active span L. The following equations are obtained:

$$\delta_4 = 2 Q L^3 / 6 E I \quad (12)$$

$$\delta_5 = ( Q L^3 \alpha^2 / 6 E I ) ( 3 - \alpha ) \quad (13)$$

$$\delta_Q = \delta_4 - \delta_5 \quad (14)$$

By applying equations (9), (12) and (13) in equation (14), hence

$$\delta_Q = Q J ( 2 - 3 \alpha^2 + \alpha^3 ) \quad (15)$$

Returning back to the original problem, the free edge of the flange does not displace but reacts against its support. To satisfy this boundary condition,  $\delta_T$  should equal  $\delta_Q$ . By equating equations (11) and (15), the following equation is obtained,

$$Q / T = ( 3 J \alpha^2 \beta - k ) / \{ J ( 2 - 3 \alpha^2 + \alpha^3 ) \} \quad (16)$$

where  $k = 1 / K_b$

This equation (16) is used to calculate prying force in T – hanger connections with snug tightened bolts.

### FINITE ELEMENT METHOD

Only quarter of the connection was modeled due to its symmetry about the X - X and Y - Y axes, **Fig. 5**. This part was divided into 540 elements. Three dimensional four node quadrilateral shell elements were used. The formulation of the element is a combination of plate bending and membrane behavior. The membrane is an isoparametric formulation including transitional in-plane stiffness components and rotational stiffness components in the direction normal to the plane of the element. The plate bending behavior includes two way

out-of-plane rotational stiffness and transitional stiffness components in the direction normal to the plane of the element. The flange thickness was made constant until the fillet. The thickness was then increased gradually until its attachment with the web. The material was modeled having modulus of elasticity  $E = 205\,000\text{ N/mm}^2$  and poisson ratio  $\nu = 0.3$ . Uniform load was applied over the web length in the positive direction of Z axis, **Fig. 5**. The bolt was modeled using 24 spring elements distributed along the perimeter of the bolt hole. They provide transitional spring support conditions having stiffness equal to the bolt axial stiffness  $K_b$  in the direction of Z axis.

### **Restraining Conditions**

Nodes were divided into three groups. Firstly, nodes lie at the planes of symmetry. Those in the X - Z plane were restrained against rotation. Only the translation in the Z axis direction is allowed. The nodes in the Y - Z plane were allowed to rotate only about the X axis. Translation is restrained in the X axis direction. Secondly, nodes lie at the hole perimeter. These were supported by the spring elements. Thirdly, nodes lie at the flange. These nodes were required to be restrained by springs having no stiffness in tension and infinity rigid in compression. This condition was satisfied by performing the analysis into steps as follows.

### **Analysis Procedure**

Initially, the analysis was performed while all the nodes of the third group were not restrained. The results were reviewed for negative displacements or reactions in the Z direction. These two cases violate the actual behavior of the connection. The restraining conditions of the nodes satisfying these two cases were modified. The translation in Z direction was restrained in the first case and allowed in the second one. The analysis was performed again with the new restraining conditions. This procedure of analyzing, reviewing the results and then modifying the restraining conditions of the nodes was continued until non of the results violate the actual behavior. At this state, the reactions of the springs were calculated. They should equal the summation of the applied force and the induced prying force. Prying force is evaluated by adding the reactions induced at the nodes of the third group that were supported against translation in the Z direction. The obtained results from the finite element analysis are presented in **Table 1** for different connections with different geometrical details. **Fig. 6** shows connection C 1 of **Table 1** after deformation.

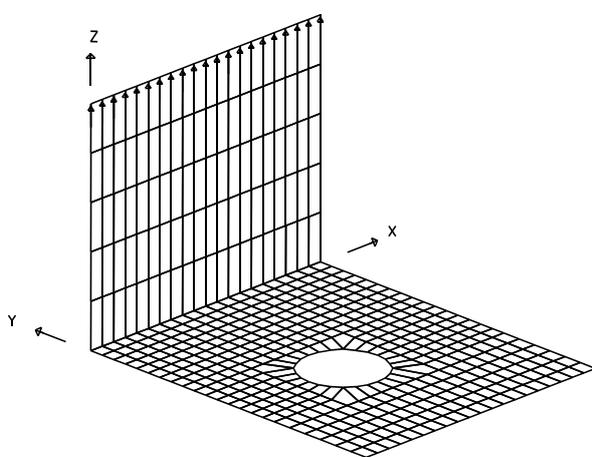


Fig. 5 Finite element mesh.

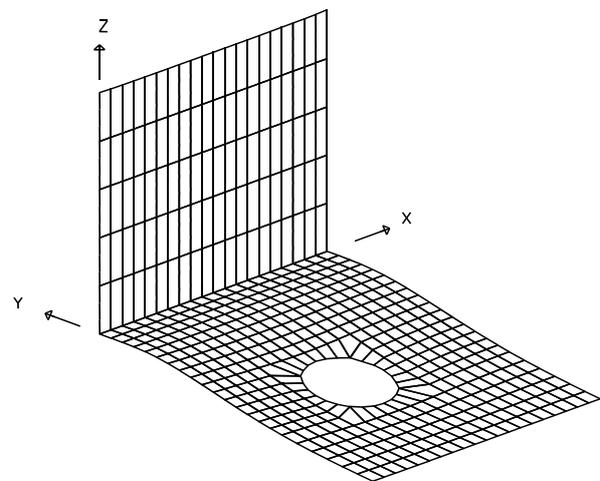


Fig. 6 Finite element result - deformation of connection C1 of table 1.

## COMPARISON OF THE RESULTS

**Fig. 7** compares between the results obtained from the finite element method and the proposed model. The problems dealt with in this figure have constant value of  $\alpha = 0.52$ . The results show good agreement up to  $J / k = 10$ . After this value, the proposed model provides conservative values for  $Q / T$  but within an acceptable margin. The consistency of the agreement between the results is examined for other values of the different parameters. Connections having different geometrical properties  $a$ ,  $b$ ,  $L$ ,  $t_f$ ,  $\alpha$ ,  $\beta$  and  $\phi$  have been studied using both the finite element method and the proposed model, **Table 1**. The obtained results confirm the agreement observed before in **Fig. 7**. The maximum difference noted is 17% in C9 at  $J / k = 58.4$ . The comparisons in general verify the adequacy of the proposed model.

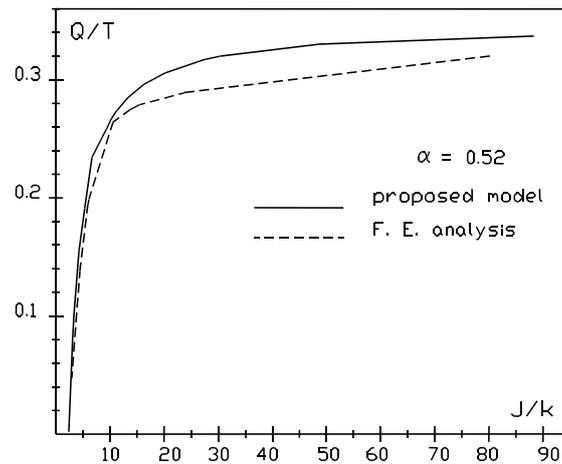


Fig. 7 Comparison between the results of the finite element analysis and the proposed model.

Table 1: Values of prying forces obtained from finite element analysis and the proposed model:

Connection details									Prying force ratio $R = Q/T$			Notes
Name	a	b	L	$t_f$	$\alpha$	$\beta$	$\phi$	J/k	$R_{F.E.}$	$R_m$	$R_m/R_{F.E.}$	
C <sub>1</sub>	30	33	63	12.7	0.476	0.523	16	15.4	0.194	0.203	105	IPE 360
C <sub>2</sub>	30	25	55	12.7	0.545	0.454	16	10.2	0.232	0.242	104	
C <sub>3</sub>	30	25	55	12.7	0.545	0.454	12	5.3	0.163	0.172	105	
C <sub>4</sub>	30	20	50	12.7	0.600	0.400	16	7.7	0.250	0.265	106	
C <sub>5</sub>	30	20	50	12.7	0.600	0.400	12	4.0	0.141	0.161	114	
C <sub>6</sub>	30	27	57	10.7	0.526	0.474	16	19.8	0.232	0.259	112	IPE 300
C <sub>7</sub>	30	27	57	10.7	0.526	0.474	12	10.3	0.211	0.224	106	
C <sub>8</sub>	30	19	49	10.2	0.612	0.388	16	14.7	0.295	0.332	113	IPE 270
C <sub>9</sub>	30	42	72	9.5	0.416	0.583	16	58.4	0.157	0.184	117	IPBI 180

## PARAMETERIC STUDY

The proposed model was used to study the effect of the different parameters on prying action. The results are presented in non dimensional forms. **Fig. 8** shows the relations between  $Q / T$ ,  $J / k$  and  $\alpha$ . The value of  $Q / T$  is significantly effected by the values of  $J / k$ . This applies up to  $J / K = 20$ . After this value, the increase in  $J / k$  value does not cause significant increase in  $Q / T$ . However, the effect of  $\alpha$  on the values of  $Q / T$  is noticeable for the different values of  $J / k$ . This indicates the importance of bolts position.

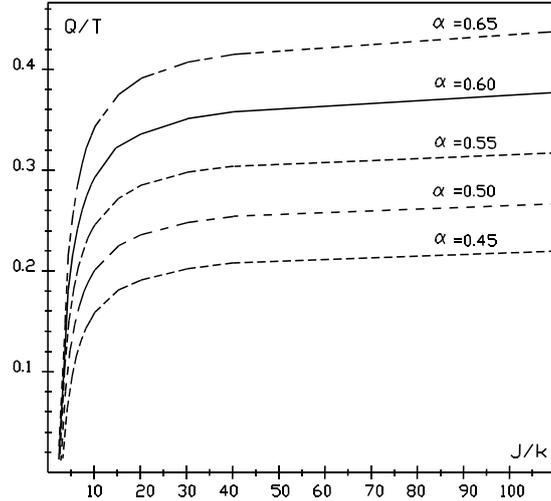


Fig. 8 Relations of  $Q/T$ ,  $J/k$  and  $\alpha$ .

**Figs. 9** and **10** show the relations between  $Q / T$ ,  $\alpha$ ,  $t_f / \phi$  and  $w / \phi$ . The following relations were used to obtain these results.

$$w = (2 e + p) / 2 \quad (17)$$

Where

$$e = \text{edge distance} = 1.5 \phi$$

$$p = \text{bolt pitch} = 3.0 \phi \text{ in figure 9 and } 6.0 \phi \text{ in figure 10 .}$$

The axial stiffness of two bolts is given by  $K = 1.6 E A_b / L_b$  in (" Eurocode 3" 1997 ). The factor 1.6 accounts for the influence of prying forces, ( Faella 1998 ). In this study, bolt axial stiffness is calculated by equation (10). The value of  $E_b$  is made equal to that of  $E$ . The value of  $L_b$  is calculated as follows :

$$L_b = t_f + R + h \quad (18)$$

Where  $R$  is the thickness of the washers and the rigid base to which the flange is connected. It is assumed to equal  $1.1 \phi$ . The  $h$  is equal to bolt head and nut depths. This is found equal to  $1.55 \phi$  for bolts of sizes up to M 22. The results show that  $Q / T$  is inversely proportional to  $t_f / \phi$ . The increase in the value of  $\alpha$  would increase the induced prying force. This is true up to  $t_f / \phi = 1.4$  and  $1.2$  in **Fig. 9** and **Fig. 10** respectively. **Fig. 11** shows the effect of a value for constant  $\alpha$ . The value of  $a$  is inversely proportional to  $Q / T$ . The use of  $a$  equal to the minimum distance required for bolt installation would produce minimum value for  $L$ . This in turn would minimize the value of the flange thickness. The comparison between **Fig. 9** and

**Fig. 10** show that The increase in flange length  $w$  reduces  $Q / T$  values. This becomes more noticeable for higher values of  $t_f / \phi$ .

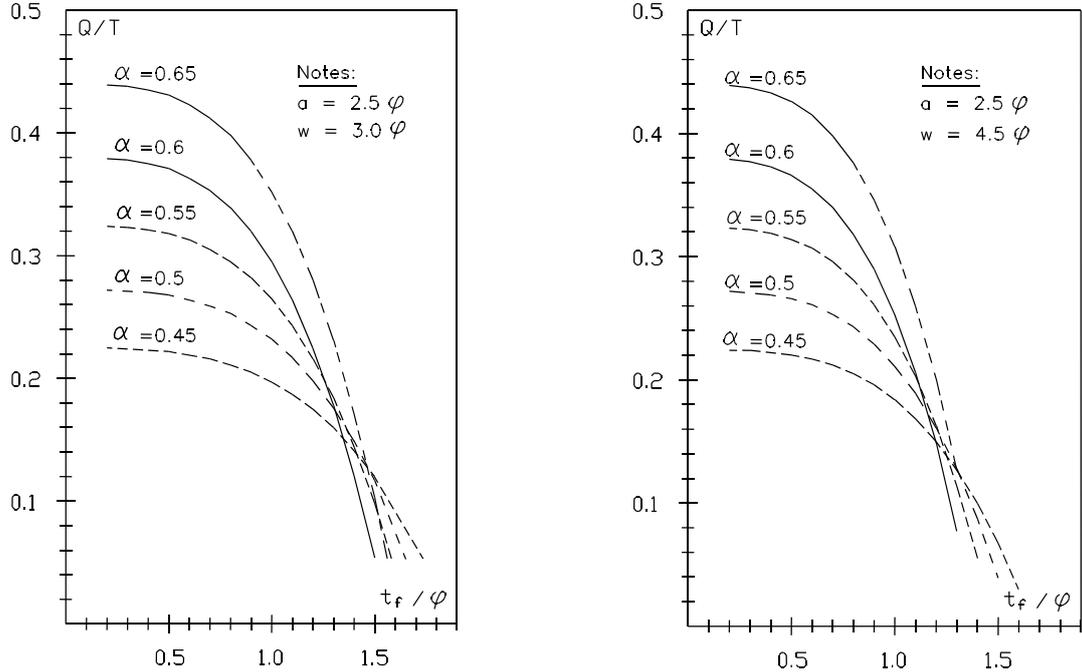


Fig. 9 Relations of  $Q/T$  ,  $t_f / \phi$  and  $\alpha$  when  $w = 3.0 \phi$ . Fig. 10 Relations of  $Q/T$  ,  $t_f / \phi$  and  $\alpha$  when  $w = 4.5 \phi$ .

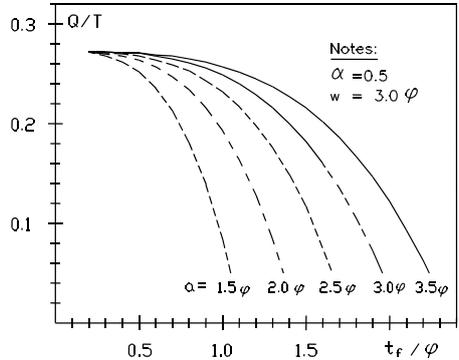


Fig. 11 Effect of  $a$  on prying forces values.

**CONDITION FOR NO PRYING ACTION**

When the following condition is satisfied, no prying force would induce.

$$3 \alpha^2 (1 - \alpha) = k / J \tag{19}$$

**Fig. 12** shows the relation between  $J / k$  and  $\alpha$  when  $Q / T = 0.0$  . The values of  $J / k$  is inversely proportional to those of  $\alpha$ . The values of  $J / k$  are limited between 2.25 and 3 for the common values of  $\alpha$  used in practice. **Fig. 13** and **14** show the relations between  $t_f / \phi$  ,  $L / \phi$  and  $\alpha$  when  $Q / T = 0$ . The following geometrical limits were used.

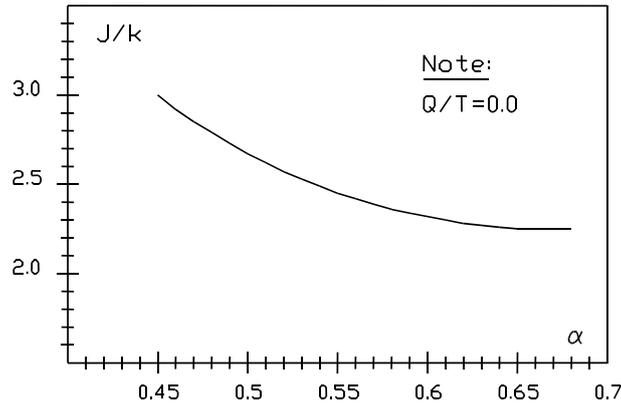


Fig. 12 Relations of  $J/k$  and  $\alpha$  when  $Q/T = 0.0$ .

$$a \geq 1.5 \phi \quad (20)$$

$$1.5 a \leq b \leq 1.5 \phi \quad (21)$$

The results indicate the following design notes. For constant value of  $L$ , the use of small value of  $\alpha$  would reduce the required thickness of the flange. On the other side, for constant value of  $t_f$ , the use of high value of  $\alpha$  would reduce the required span  $L$ . The increase in  $w$  would reduce  $t_f$ .

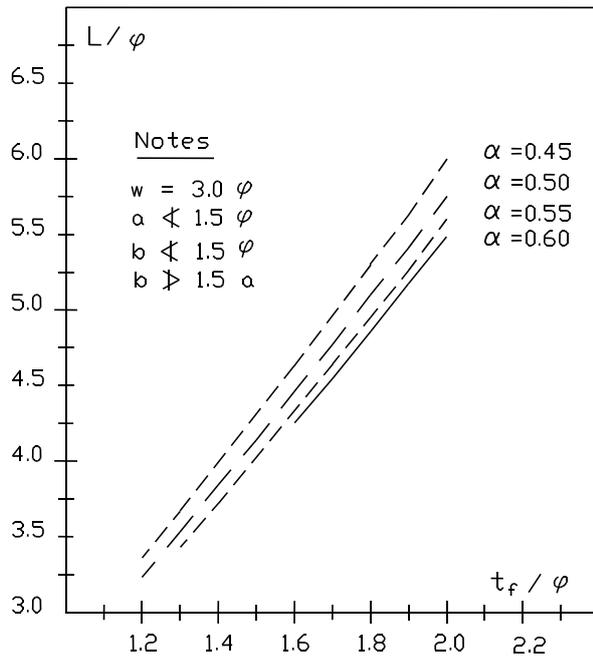


Fig 13 Relations of  $L/\phi$ ,  $t_f/\phi$  and  $\alpha$  when  $w = 3.0 \phi$ .

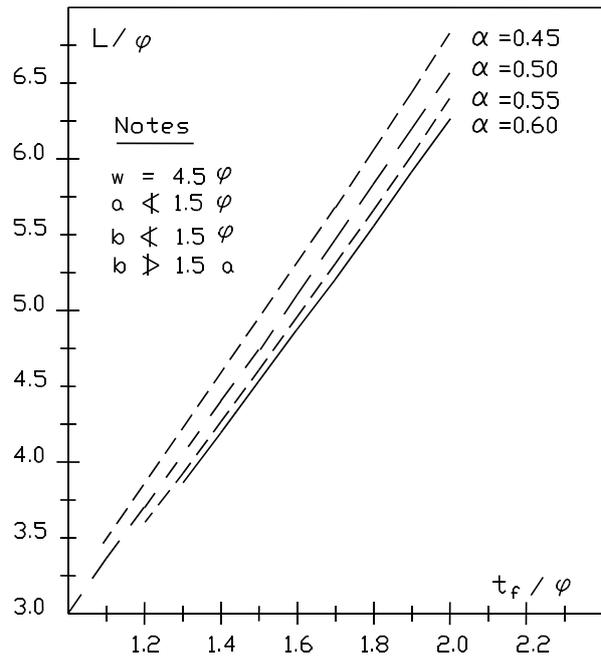


Fig 14 Relations of  $L/\phi$ ,  $t_f/\phi$  and  $\alpha$  when  $w = 4.5 \phi$ .

### PROPOSED DESIGN PROCEDURE

This is a working load method.

- 1- Assume that  $Q/T = 20\%$
- 2- Load per bolt =  $P_i = \text{applied tension load} * 1.2/4$
- 3- Define bolt diameter and grade so that :  
load per bolt / allowable bolt load  $\leq 1$

- 4- The values of  $a$  and  $w$  are dictated by installation requirements. Otherwise, it is better to reduce  $a$  and increase  $w$  as far as the specifications allow.
- 5- The value of  $t_f$  and  $L$  can be chosen according to the geometrical dimensions of the available sections.
- 6- The use of **Fig. 9** and **Fig. 10** would make the proportion of the different elements of the connection easier. However, their limitations should be satisfied. Similar figures can be obtained for other limits. The intersection of the perpendiculars at  $Q / T = 0.2$  and  $T_f / \phi$  value would define the required  $\alpha$
- 7- When  $L > (a / \alpha)$ , the following can be made:
  - i - reduce the value of  $t_f / \phi$ .
  - ii- obtain the actual value of  $Q / T$  at these conditions and hence the value of  $P_f$ . The difference between  $P_i$  and  $P_f$  is considered as a reserve strength in the bolt.
- 8- The flange is treated as a cantilever having a span  $L$  and subjected to concentrated loads  $P_f$  and  $Q$  at points B and A respectively. The stresses at the end of the span should not exceed the allowable stresses in the codes.

When considering the case of design for no prying forces, the above steps are applied. However,  $P =$  applied tension force / 4. **Figs. 13** and **14** are used. The intersection of the perpendiculars at  $t_f / \phi$  and  $L / \phi$  would define the required value of  $\alpha$ .

### Example

Consider the T – hanger connection designed in example 11 –1 in the manual of the (AISC 1980). The prying force is calculated using the proposed model and compared to the value presented in the manual. The available data are:

$$T = 90 \text{ KN}$$

$$G = 181.0 \text{ mm}, t_f = 18.2 \text{ mm}, t_w = 10.9 \text{ mm}, w = 100.0 \text{ mm}$$

$$\phi = 20.0 \text{ mm}, R = 22.2 \text{ mm} + 6 \text{ mm}$$

$$\text{The distance between the bolts center to center} = 100.0 \text{ mm}$$

### Solution

By assuming that  $r = 12.5 \text{ mm}$ ,  $h = 30 \text{ mm}$  and  $E = E_b$

$$b = \frac{181 - 100}{2} = 40.5 \text{ mm}$$

$$a = \frac{100 - (10.9 + 12.5 * 2)}{2} = 32 \text{ mm}$$

$$L = a + b = 72.5 \text{ mm}$$

Then :  $\alpha = 0.441$  &  $\beta = 0.559$

From equation (9), (10), (18)  $L_b = 18.2 + 22.2 + 30 = 76.4 \text{ mm}$ ,  $j/k = 5.20$

By using the values of  $\alpha$ ,  $\beta$  and  $j/k$  in equation (16)

$$Q/T = \{3 (0.441)^2 (0.559) - (5.2)^{-1}\} / \{2 - 3 (0.441)^2 + (0.441)^3\} = 0.09$$

Hence  $Q = 8.1 \text{ KN}$ . The value presented in the manual of (AISC 1980) is  $Q = 10.7 \text{ KN}$ . The difference in  $Q$  values refers to the different assumptions used.

## **CONCLUSION**

A simple model for evaluating prying forces in T - hanger connections with snug tightened bolts is proposed. The model includes all the parameters that affect the flexural stiffness of the flanges and the axial stiffness of the bolts. It is valid as far as the connection behaves in an elastic manner. The finite element method was also used to model the behaviour of T - hanger connections. The prying forces' values obtained from the finite element analysis were compared to those from the proposed model. The results show good agreement and verify the adequacy of the proposed model. The ratio of the flange flexural stiffness to bolt axial stiffness affects the magnitude of prying forces. The increase in the value of this ratio would reduce the induced prying forces values. This can be carryout by increasing the flange thickness and length and/or reducing the flange span. Bolts position is another significant factor that affecting prying forces values. When using the distance between bolt hole centre and the web equal to the minimum distance required for bolt installation, minimum prying force would induce. Design procedure is proposed.

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## NOMENCLATURE

$A_b$	bolt cross sectional area.
$a, b$	distances define the position of bolts holes in the flanges.
$E$	modulus of elasticity of the flange material.
$E_b$	modulus of elasticity of the bolts material.
$e$	edge distance.
$G$	flange width.
$h$	depths of bolt head and nut.
$K, K_b$	bolts axial stiffness
$L$	flange span.
$L_b$	bolt grip length.
$P$	total applied tension load.
$p$	bolt pitch
$Q$	prying force
$R$	thickness of washers and rigid base.
$r$	fillet radius.
$T$	applied tension force per bolt.
$t_f$	flange thickness.
$t_w$	web thickness.
$w$	flange length per bolt.
$\alpha, \beta$	ratios.
$\delta_1, \delta_2, \delta_T$	deflections due to applied tension load.
$\delta_3$	spring elongation.
$\delta_4, \delta_5, \delta_Q$	deflections due to induced prying force.
$\phi$	bolt diameter.
$\nu$	poison ratio.